



## Application of Fuzzy Logic to Capital Budgeting Decisions; Case Study Research

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Received; 15 November 2016 Accepted; 29 November 2016; © The author(s) 2016. Published with open access at [www.questjournals.org](http://www.questjournals.org)

**ABSTRACT:** This paper presents a model for capital budgeting decisions made by corporations. Capital budgeting decisions are based on various methods: NPV, IRR, MIRR, payback period, discounted payback period, etc. There hasn't been any model in capital budgeting decisions which takes multiple methods into consideration until now. Fuzzy logic is a superset of Aristotle's logic which has been enlarged to manage the concept of partial truth-truth values between "completely true" and "completely false". As its name expresses, it is the logic based on way of reasoning which are approximate rather than exact. In the research, we have defined one fuzzy output (quality of investment) and three fuzzy inputs: net present value, internal rate of return, modified internal rate of return.

**Keywords:** NPV, IRR, MIRR, fuzzy input, fuzzy output.

### I. INTRODUCTION

Capital budgeting is the process by which the businesses define how to invest their capital. The different methods are used in capital budgeting decisions. They are divided into two groups: discounted cash flow based methods and non-discounted cash flow based methods. The NPV, MIRR, IRR and discounted payback period are most frequently employed in the evaluation of investment projects. Actually, the decisions made by businesses are based on a single indicator. However, there are some situations where conflict of NPV and IRR, NPV and MIRR, MIRR and IRR methods occurs when they produce opposite results. We have applied fuzzy logic into capital budgeting decisions to join the methods into a single IRR\_MIRR\_NPV method. NPV is the value which is calculated by the difference between discounted cash inflows and outflows at given cost of capital. If the NPV is greater than or equal to 0, this investment project should be accepted. IRR is the rate in which net present value of investment is equal to 0. If IRR is greater than the given cost of capital, the investment project should be accepted. MIRR is the rate which makes future value of cash flows equal to the present value of cash flows where cash inflows are reinvested.

### II. LITERATURE REVIEW

Fuzzy Logic was introduced in 1965 by Lotfi A. Zadeh, professor at the University of California in Berkeley. Fuzzy Logic is a logic which allows intermediate values to be defined between conventional evaluations like true/false, good/bad, etc. Concepts like bad or very good can be quantified mathematically and processed by smart computers, for applying human-like way of thinking in the programming.

In capital budgeting decision making, the methods sometimes produces opposite results. These types of problems have been investigated by many researchers including: Brealey, Myers, Marcus, Blank, and Brigham. However, it has not been studied effectively yet.

### III. ANALYSIS OF CAPITAL BUDGETING METHODS

#### 3.1 Comparison Of The Methods

Hypothetically, the Mati Company has 5 different capital projects. All the projects require initial investment which is in range from \$8933 to \$11744. In table 1, the values at time  $t_0$  represents the initial investment. It is presupposed that all projects will generate some revenues in next 9 years. All the values related to cash flows were randomly generated via Excel's "randbetween" function. Intentionally, the values have been manipulated to create the case in which NPV, IRR, and MIRR results are relevant to our decision. The given table represents the data on cash flows for five individual projects.

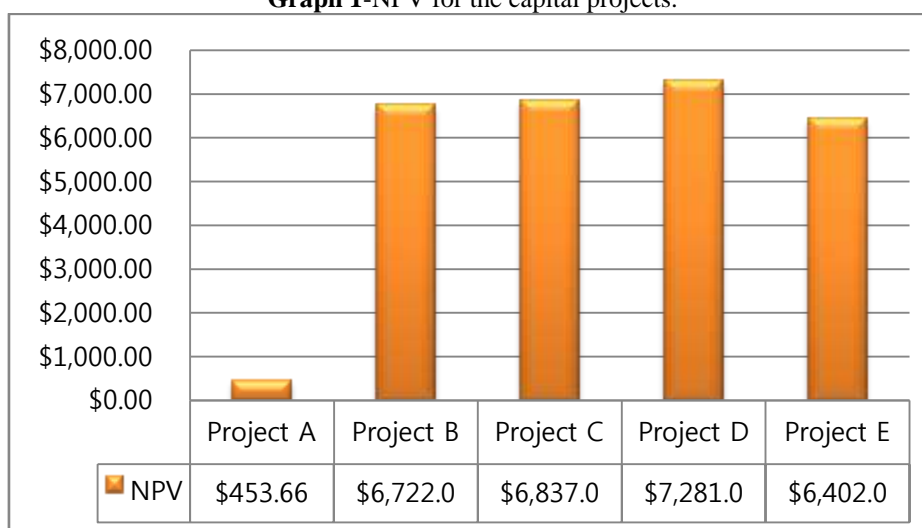
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**Table 1-**Cash flows from the capital projects

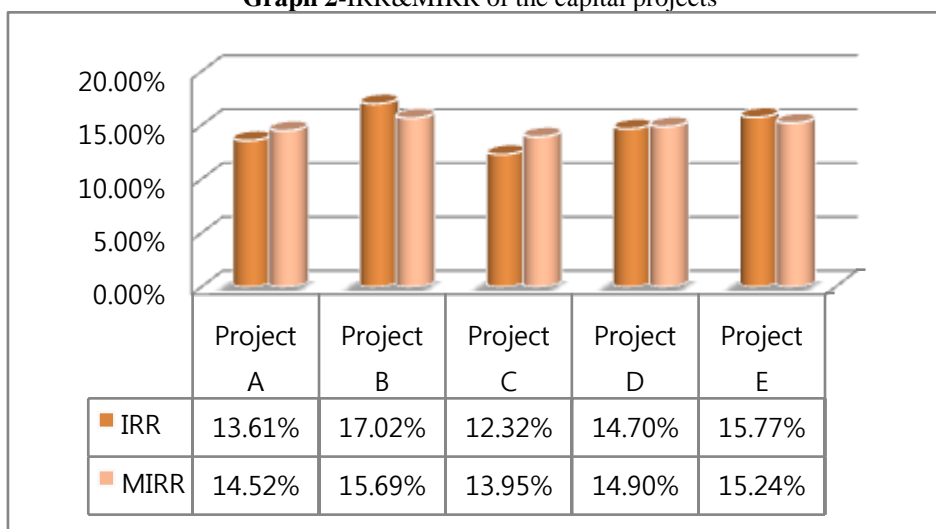
Years/Projects	Project A	Project B	Project C	Project D	Project E
0	-11081.00	-8933.00	-11744.00	-11559.00	-10878.00
1	4352.00	4769.00	3190.00	4724.00	5441.00
2	3039.00	1606.00	2671.00	3232.00	3066.00
3	2010.00	1080.00	2876.00	1505.00	1462.00
4	1015.00	1149.00	1932.00	1545.00	1165.00
5	1721.00	1459.00	1709.00	1795.00	1461.00
6	1145.00	1003.00	1388.00	1658.00	1259.00
7	1378.00	1895.00	1468.00	1340.00	1212.00
8	1537.00	1398.00	1598.00	1495.00	1115.00
9	1121.00	1296.00	1749.00	1546.00	1099.00

Accepting the cost of capital as 12%, and reinvestment rate as 10%, we have calculated the net present values, IRR and MIRR of the projects. According to the graph 1, all the projects have positive net present values. In addition, IRR of all the projects is greater than cost of capital. Modified internal rate of return is also greater than the cost of capital for all projects.

**Graph 1-**NPV for the capital projects.



**Graph 2-**IRR&MIRR of the capital projects



### 3.2 Defining fuzzy variables

In the model, we have defined “quality of investment” as an output variable. Input variables are net present value (NPV), internal rate of return (IRR), and modified internal rate of return (MIRR). Fuzzy output variable assesses the level of quality of investment decision for the projects. It is supposed that quality of investment can be “Low”, “Normal” and “Good”. Quantification of the scores for output variable is in range from 0 to 10. First fuzzy input variable is the net present value of projects which is the most common method used by finance m

managers when evaluating the capital budgeting decisions. It is supposed that NPV can be “Small”, “Medium” and “Large”. Quantification of the scores for input variable, NPV is in range from \$0 to \$7300. Second fuzzy input variable is the internal rate of return for the projects. It is supposed that IRR can be “Small”, “Medium” and “Large”. Quantification of the scores for input variable, IRR is in range from 0% to 18%. Third fuzzy input variable is the modified internal rate of return for the projects. It is supposed that MIRR can be “Small”, “Medium” and “Large”. Quantification of the scores for input variable, MIRR is in range from 0% to 11%.

### 3.3 Fuzzy Logic

Fuzzy logic is based on fuzzy sets. It enables making decision based on incomplete information, and models are based on “if-and-then” rules. When we assume that  $a = [a_1, a_2, \dots, a_n]$  is a vector of features describing any object or state and  $b = [b_1, b_2, \dots, b_m]$  is the vector of output values of a system, the rules are represented in the form: *IF  $a_1$  is  $A_{r1}$  AND  $a_2$  is  $A_{r2}$  AND... AND  $a_n$  is  $A_{rn}$  THEN  $b_1$  is  $B_{r1}$ ,  $b_2$  is  $B_{r2}$ ...  $b_m$  is  $B_{rm}$  where:  $a \in A = a_1 \times a_2 \times \dots \times a_n$ ,  $b \in B = b_1 \times b_2 \times \dots \times b_m$  and  $A_r = A_{r1} \times A_{r2} \times \dots \times A_{rn} \subseteq A$ ,  $B_r = B_{r1} \times B_{r2} \times \dots \times B_{rm} \subseteq B$  are the fuzzy.*

**We define algorithms for approximate reasoning in fuzzy logic. Approximate algorithms for projects in this paper consists the following rules:**

1. NPV is small: if the IRR is low, and MIRR is low, then quality of investment is low.
2. NPV is small: if the IRR is low, and MIRR is medium, then quality of investment is low.
3. NPV is small: if the IRR is low, and MIRR is high, then quality of investment is low.
4. NPV is small: if the IRR is medium, and MIRR is low, then quality of investment is low.
5. NPV is small: if the IRR is medium, and MIRR is medium, then quality of investment is normal.
6. NPV is small: if the IRR is medium, and MIRR is high, then quality of investment is normal.
7. NPV is small: if the IRR is high, and MIRR is low, then quality of investment is low.
8. NPV is small: if the IRR is high, and MIRR is medium, then quality of investment is normal.
9. NPV is small: if the IRR is high, and MIRR is high, then quality of investment is high.
10. NPV is medium: if the IRR is low, and MIRR is low, then quality of investment is low.
11. NPV is medium: if the IRR is low, and MIRR is medium, then quality of investment is normal.
12. NPV is medium: if the IRR is low, and MIRR is high, then quality of investment is normal.
13. NPV is medium: if the IRR is medium, and MIRR is low, then quality of investment is normal.
14. NPV is medium: if the IRR is medium, and MIRR is medium, then quality of investment is normal.
15. NPV is medium: if the IRR is medium, and MIRR is high, then quality of investment is normal.
16. NPV is medium: if the IRR is high, and MIRR is low, then quality of investment is normal.
17. NPV is medium: if the IRR is high, and MIRR is medium, then quality of investment is normal.
18. NPV is medium: if the IRR is high, and MIRR is high, then quality of investment is high.
19. NPV is large: if the IRR is low, and MIRR is low, then quality of investment is low.
20. NPV is large: if the IRR is low, and MIRR is medium, then quality of investment is normal.
21. NPV is large: if the IRR is low, and MIRR is high, then quality of investment is high.
22. NPV is large: if the IRR is medium, and MIRR is low, then quality of investment is normal.
23. NPV is large: if the IRR is medium, and MIRR is medium, then quality of investment is normal.
24. NPV is large: if the IRR is medium, and MIRR is high, then quality of investment is high.
25. NPV is large: if the IRR is high, and MIRR is low, then quality of investment is high.
26. NPV is large: if the IRR is high, and MIRR is medium, then quality of investment is high.
27. NPV is large: if the IRR is high, and MIRR is high, then quality of investment is high.

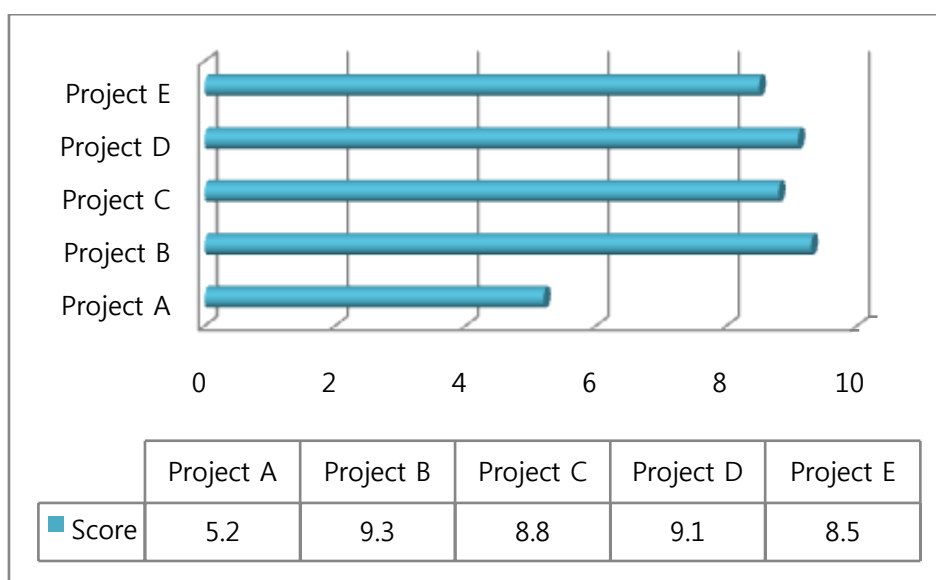
### 3.4 Defuzzification and results

We have used MATLAB in this project for defuzzification purposes. This is last step in fuzzy logic, which allows formulating aggregation of results from fuzzy sets to a single decision. There are many methods of defuzzification. The most frequently used methods includes: bisector of area, first of maximum, fuzzy clustering defuzzification, random choice of maximum, center of gravity. We have applied COG (center of gravity). It calculates area under the membership function. The value  $x^*$  of the output, which is resulting from the COG method, is given in the following equation. Where the  $\mu(x_i)$  is membership function. The formula shows that COG calculates the expected value when it is considered to be probability distribution.

$$x^* = \frac{\sum_{i=1}^n x_i \cdot \mu(x_i)}{\sum_{i=1}^n \mu(x_i)}$$

Intentionally, we don't include all the steps in our article. The results of the assessment of the investment quality of the capital projects are shown in the Graph 3.

**Graph 3-Final scores for the capital projects.**



According to the results, Project B is the best choice, and should be invested firstly. The ranking for the project's quality of investment is B, D, C, E, A. These scores are calculated using fuzzy logic which includes three methods based on discounted cash flows.

#### IV. CONCLUSION

We have applied fuzzy logic into the investment decision making methods. Every method has some weaknesses like; NPV does not show the effectiveness of an investment project, IRR is not suitable for rating the projects for their profitability. New applications should be developed to decrease uncertainty and risk of the project. Being first paper in this topic, we have touched only limited sides of the problem. This article presents a new way of modeling and evaluation of the projects based on the following criteria: net present value, internal rate of return, modified internal rate of return using the fuzzy sets theory, which allows solving problems that contain uncertainty, subjectivity, and ambiguity. This model can be used by analysts to make decisions in related issues.

#### ACKNOWLEDGEMENT

I would like to express my special thanks of gratitude to my friends who helped me a lot in finalizing this research financially. I sincerely thank my mother for her encouragement in carrying out all my project works. Last, but not least, the unknown one was also an important inspiration for me. I dedicate this article to co-authors' families. (Nahid Shirinov)

#### REFERENCES

- [1]. Guanrong Chen, Trung Tat Pham, "Introduction to fuzzy sets, fuzzy logic and fuzzy control systems", CRC press LLC, 2001.
- [2]. L.A.Zadeh, "Fuzzy sets, information and control", 1965.
- [3]. L.A.Zadeh, "Making computers think like people", 1984.
- [4]. Stojic Gordan, "Modeling evaluation of the size of countries using fuzzy logic", Journal of Geographic's Pannonica, June 2010
- [5]. Simon Gervais, "Capital budgeting and other investment decisions", Duke University, November 2009
- [6]. Bierman and Smith, "The capital budgeting decision: economic analysis of investment projects", Prentice Hall, 1993.
- [7]. Booth R, "Avoiding pitfalls in investment appraisal", Journal of Management Accounting, November 1999
- [8]. Brealey and Myers, "Principles of corporate finance", McGraw-Hill/Irwin, 2003.
- [9]. Ross, Westerfield, Jaffe, "Corporate finance", McGraw-Hill/Irwin, 2002
- [10]. Ibrahim Ahmed, "Factors determining the selection of capital budgeting techniques", Journal of Finance and Investment Analysis, 2013.