



Research Paper

# A Systematic Approach to Statistical Computation: A Comparative Guide to Measures of Central Tendency and Dispersion

Chetna Rani Gupta

Assistant Prof. in Mathematics  
 Multani Mal Modi College, Patiala, Punjab

## Abstract

Data literacy forms the backbone of contemporary professional fields, ranging from healthcare to technology. However, a persistent challenge in statistics education is that learners often grasp the conceptual purpose of measures of central tendency and dispersion but struggle with the mathematical execution. Assuming that students already possess the necessary foundational theoretical background, this paper serves as a comparative guide focused entirely on moving from concept to computation. It demonstrates the application of formulas for these key metrics—mean, median, mode, mean deviation, and standard deviation—by tracing all calculations through a single, consistent baseline dataset, appropriately modified for Individual, Discrete, and Continuous series.

**Keywords:** Mean, Median, Mode, Mean deviation, and Standard deviation

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## I. INTRODUCTION

Statistics is the language of modern problem-solving, and proficiency in calculating measures of central tendency and dispersion is a foundational requirement for data analysis across various academic and professional disciplines. However, a pedagogical challenge persists: students often develop strong conceptual understandings but lack procedural fluency. The transition from theoretical knowledge to accurate formula application frequently devolves into rote memorization rather than analytical problem-solving. This paper focuses on moving from concept to computation, emphasizing the precise understanding and comparative application of specific formulas required for different types of numerical problems. To facilitate clear comparative insight, a single, consistent dataset is utilized as a running example, appropriately adapted across Individual, Discrete, and Continuous series. By applying formulas for central tendency (mean, median, and mode) and dispersion (mean deviation and standard deviation), the methodology highlights the logical, sequential flow of the calculations. The goal is to shift the student's mindset from memorizing isolated formulas to executing logical, step-by-step procedures, ultimately fostering true competence in statistical computation.

## II. ARITHMETIC MEAN

### Notation and terminology used

|           |                                                                                       |
|-----------|---------------------------------------------------------------------------------------|
| $X$       | the series                                                                            |
| $x$       | the terms of the series $X$                                                           |
| $\bar{X}$ | Arithmetic mean of the series $X$                                                     |
| $n$       | number of terms of the series $X$                                                     |
| $A$       | the assumed mean of the series $X$ ,                                                  |
| $d$       | the deviation from assumed mean $d = X - A$ for individual series and discrete series |
| $c$       | the common factor of the series $d$ and $d' = \frac{X-A}{c}$                          |
| $d'$      | $d' = \frac{X - A}{c}$                                                                |
| $f$       | the frequency of the series $X$                                                       |

|                                     |                                                                                             |
|-------------------------------------|---------------------------------------------------------------------------------------------|
| $N = \sum f$                        | The sum of frequencies, where $f$ is the frequency                                          |
| $m$                                 | the mid-values of the class interval of a continuous series                                 |
| $d = m - A, d' = \frac{m-A}{c}$     | In case of a continuous series, deviation of the mid values are taken from the assumed mean |
| $\overline{X}_w$                    | Weighted Arithmetic Mean                                                                    |
| $d = X - A_w, d' = \frac{X-A_w}{c}$ | deviation of the mid values are taken from the Assumed Weighted Arithmetic Mean             |

|                                                                                             |                                                                                                                          |                                                                                                                                                                      |
|---------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Arithmetic Mean in case of an Individual Series</b>                                      |                                                                                                                          |                                                                                                                                                                      |
| Direct Method<br>$\overline{X} = \frac{\sum x}{n}$                                          | Short-Cut Method<br>$\overline{X} = A + \frac{\sum d}{n}$                                                                | Step Deviation Method<br>$\overline{X} = A + \frac{\sum d'}{n} \times c$                                                                                             |
| <b>Arithmetic Mean in case of Discrete Series</b>                                           |                                                                                                                          |                                                                                                                                                                      |
| Direct Method<br>$\overline{X} = \frac{\sum fx}{N}$                                         | Short-Cut Method<br>$\overline{X} = A + \frac{\sum fd}{N}$                                                               | Step Deviation Method<br>$\overline{X} = A + \frac{\sum fd'}{N} \times c$                                                                                            |
| <b>Arithmetic Mean in case of Continuous Series</b>                                         |                                                                                                                          |                                                                                                                                                                      |
| Direct Method<br>$\overline{X} = \frac{\sum fm}{N}$                                         | Short-Cut Method<br>$\overline{X} = A + \frac{\sum fd}{N}$                                                               | Step Deviation Method<br>$\overline{X} = A + \frac{\sum fd'}{N} \times c$                                                                                            |
| <b>Weighted Arithmetic Mean</b>                                                             |                                                                                                                          |                                                                                                                                                                      |
| Direct Method<br>$\overline{X}_w = \frac{\sum wx}{\sum w}$                                  | Short-Cut Method<br>$\overline{X}_w = A_w + \frac{\sum wd}{\sum w}$                                                      | Step Deviation Method<br>$\overline{X} = A_w + \frac{\sum wd'}{\sum w} \times c$                                                                                     |
| <b>Combined Arithmetic Mean</b>                                                             |                                                                                                                          |                                                                                                                                                                      |
| In case of two series<br>$X_{12} = \frac{N_1\overline{X}_1 + N_2\overline{X}_2}{N_1 + N_2}$ | In case of three series<br>$X_{123} = \frac{N_1\overline{X}_1 + N_2\overline{X}_2 + N_3\overline{X}_3}{N_1 + N_2 + N_3}$ | In case of n series<br>$X_{123 \dots n} = \frac{N_1\overline{X}_1 + N_2\overline{X}_2 + N_3\overline{X}_3 \dots + N_n\overline{X}_n}{N_1 + N_2 + N_3 + \dots + N_n}$ |
| <b>Corrected Arithmetic Mean</b>                                                            |                                                                                                                          |                                                                                                                                                                      |
| Corrected $\sum x$ = incorrect $\sum x$ - incorrect values $x$ + corrected values $x$       |                                                                                                                          |                                                                                                                                                                      |
| Apply the formula $\overline{X} = \frac{\text{corrected } \sum x}{n}$                       |                                                                                                                          |                                                                                                                                                                      |

**Note :** Observe that the foundational approach to computing the arithmetic mean remains consistent across Individual, Discrete, and Continuous series. The primary distinction lies in how the specific components namely  $n, N, d, d'$  are derived for each data type. Furthermore, while the Individual series lacks frequencies, both Discrete and Continuous series require multiplying values by their respective frequencies. Lastly, a notational difference exists in the direct method: the Continuous series employs  $\sum fm$ , whereas the Discrete series relies on  $\sum fx$

### 2.1 Example: Individual series

|     |                         |                                    |                                                                                           |                                                                                                                    |                                                                                                                                            |
|-----|-------------------------|------------------------------------|-------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------|
| $X$ | $A = 25$<br>$d = m - A$ | $c = 10$<br>$d' = \frac{m - A}{c}$ | Direct Method<br>$\overline{X} = \frac{\sum x}{n}$<br>$\overline{X} = \frac{180}{6} = 30$ | Short-Cut Method<br>$\overline{X} = A + \frac{\sum d}{n}$<br>$\overline{X} = 25 + \frac{30}{6}$<br>$= 25 + 5 = 30$ | Step Deviation Method<br>$\overline{X} = A + \frac{\sum d'}{n} \times c$<br>$\overline{X} = 25 + \frac{3}{6} \times 10$<br>$= 25 + 5 = 30$ |
| 5   | -20                     | -2                                 |                                                                                           |                                                                                                                    |                                                                                                                                            |
| 15  | -10                     | -1                                 |                                                                                           |                                                                                                                    |                                                                                                                                            |

|                |               |                |  |  |  |
|----------------|---------------|----------------|--|--|--|
| 25             | 0             | 0              |  |  |  |
| 35             | 10            | 1              |  |  |  |
| 45             | 20            | 2              |  |  |  |
| 55             | 30            | 3              |  |  |  |
| $\Sigma x=180$ | $\Sigma d=30$ | $\Sigma fd'=3$ |  |  |  |

## 2.2 Example: Discrete series

| $X$                                                                                           | Frequency ( $f$ ) | $Xf$             | $A = 25$<br>$d = X - A$                                                                                              | $fd$            | $c = 10'$<br>$\frac{d}{c} = \frac{x - A}{c}$                                                                                                           | $fd'$            |
|-----------------------------------------------------------------------------------------------|-------------------|------------------|----------------------------------------------------------------------------------------------------------------------|-----------------|--------------------------------------------------------------------------------------------------------------------------------------------------------|------------------|
| 5                                                                                             | 5                 | 25               | -20                                                                                                                  | -100            | -2                                                                                                                                                     | -10              |
| 15                                                                                            | 4                 | 60               | -10                                                                                                                  | -40             | -1                                                                                                                                                     | -4               |
| 25                                                                                            | 3                 | 75               | 0                                                                                                                    | 0               | 0                                                                                                                                                      | 0                |
| 35                                                                                            | 2                 | 70               | 10                                                                                                                   | 20              | 1                                                                                                                                                      | 2                |
| 45                                                                                            | 7                 | 315              | 20                                                                                                                   | 140             | 2                                                                                                                                                      | 14               |
| 55                                                                                            | 9                 | 495              | 30                                                                                                                   | 270             | 3                                                                                                                                                      | 27               |
|                                                                                               | $\Sigma f=30$     | $\Sigma fm=1040$ |                                                                                                                      | $\Sigma fd=290$ |                                                                                                                                                        | $\Sigma fd' =29$ |
| Arithmetic Mean by Direct Method<br>$\bar{X} = \frac{\Sigma fx}{N} = \frac{1040}{30} = 34.67$ |                   |                  | Arithmetic Mean by Short-Cut Method<br>$\bar{X} = A + \frac{\Sigma fd}{N} = 25 + \frac{290}{30} = 25 + 9.67 = 34.67$ |                 | Arithmetic Mean by Step Deviation Method<br>$\bar{X} = A + \frac{\Sigma fd'}{N} \times c$<br>$= 25 + \frac{29}{30} \times 10$<br>$= 25 + 9.67 = 34.67$ |                  |

## 2.3 Example: Continuous series covering mean only by applying all the three methods Direct, Short Cut and Step Deviation method

2.4 in the above example if the series  $X$  is replaced by the class intervals and value  $x$  is replaced by the mid- points  $m$  then the new series so obtained will represent continuous series and same results will hold true for the continuous series obtained so

## III. QUARTILES, DECILES AND PERCENTILES

### Notation and terminology used

Quartiles, Deciles, Percentiles are represented by  $Q_i$ ,  $D_i$  and  $P_i$  respectively, rest are same as that of Arithmetic Mean.  $Q_2$  is also known as Median represented as  $M$

|                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                   |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Quartiles $Q_i$ where $1 \leq i \leq 3$                                                                                                                                                                                                                                                                                                                                                                                                                 | Deciles $D_i$ where $1 \leq i \leq 10$                                                                                                                                                                                                                                                                                                                                                                                                        | Percentile $P_i$ where $1 \leq i \leq 100$                                                                                                                                                                                                                                                                                                                                                                                                        |
| <b>Quartiles, Deciles and percentiles in case of Individual series</b>                                                                                                                                                                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                   |
| In all cases first of all arrange data in ascending or descending order                                                                                                                                                                                                                                                                                                                                                                                 |                                                                                                                                                                                                                                                                                                                                                                                                                                               |                                                                                                                                                                                                                                                                                                                                                                                                                                                   |
| $Q_i = \text{value of } \frac{i(n+1)}{4} \text{th term}$<br><br>When $\frac{i(n+1)}{4}$ is whole number say $a$ then $Q_i$ is equal to the value of $a^{\text{th}}$ term of the series<br><br>If $\frac{i(n+1)}{4}$ is in decimal say $a.b$ then<br>$Q_i = a^{\text{th term}} + 0.b((a+1)^{\text{th}} - a^{\text{th term}})$<br><br>If $\frac{i(n+1)}{4}$ is in decimal say $a.5$ then<br>$Q_i = \frac{a^{\text{th term}} + (a+1)^{\text{th term}}}{2}$ | $D_i = \text{value of } \frac{i(n+1)}{10} \text{th term}$<br><br>When $\frac{i(n+1)}{10}$ is whole number say $a$ then $D_i$ is equal to the value of $a^{\text{th}}$ term<br><br>If $\frac{i(n+1)}{10}$ is in decimal say $a.b$ then<br>$D_i = a^{\text{th term}} + 0.b((a+1)^{\text{th}} - a^{\text{th term}})$<br><br>If $\frac{i(n+1)}{10}$ is in decimal say $a.5$ then<br>$D_i = \frac{a^{\text{th term}} + (a+1)^{\text{th term}}}{2}$ | $P_i = \text{value of } \frac{i(n+1)}{100} \text{th term}$<br><br>When $\frac{i(n+1)}{100}$ is whole number say $a$ then $P_i$ is equal to the value of $a^{\text{th}}$ term<br><br>If $\frac{i(n+1)}{100}$ is in decimal say $a.b$ then<br>$P_i = a^{\text{th term}} + 0.b((a+1)^{\text{th}} - a^{\text{th term}})$<br><br>If $\frac{i(n+1)}{100}$ is in decimal say $a.5$ then<br>$P_i = \frac{a^{\text{th term}} + (a+1)^{\text{th term}}}{2}$ |

|                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         |                                                   |                                                    |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------|----------------------------------------------------|
| <b>Quartiles, Deciles and percentiles in case of Discrete series</b>                                                                                                                                                                                                                                                                                                                                                                                                                                    |                                                   |                                                    |
| In all cases first of all arrange data in ascending or descending order<br>$Q_i$ = value of $\frac{i(N+1)}{4}$ th term, $D_i$ = value of $\frac{i(N+1)}{10}$ th term, $P_i$ = value of $\frac{i(N+1)}{100}$ th term<br>Locate the cumulative frequency which is equal to or next higher to value of $\frac{i(N+1)}{4}$ th / $\frac{i(N+1)}{10}$ th term / $\frac{i(N+1)}{100}$ th term. Corresponding to this, locate the Quartile/Decile/percentile in the given series                                |                                                   |                                                    |
| <b>Quartiles, Deciles and percentiles in case of continuous series</b>                                                                                                                                                                                                                                                                                                                                                                                                                                  |                                                   |                                                    |
| In all cases first of all arrange data in ascending or descending order<br>$Q_i$ = value of $\frac{iN}{4}$ th term, $D_i$ = value of $\frac{iN}{10}$ th term, $P_i$ = value of $\frac{iN}{100}$ th term<br>Locate the cumulative frequency which is equal to or next higher to value of $\frac{iN}{4}$ th / $\frac{iN}{10}$ th term / $\frac{iN}{100}$ th term. Corresponding to this, locate the Quartile/Decile/percentile class and apply the corresponding following formula                        |                                                   |                                                    |
| $Q_i = L + \frac{\frac{iN}{4} - cf}{f} \times h$                                                                                                                                                                                                                                                                                                                                                                                                                                                        | $D_i = L + \frac{\frac{iN}{10} - cf}{f} \times h$ | $P_i = L + \frac{\frac{iN}{100} - cf}{f} \times h$ |
| L is the lower limi of Quartile/Decile/percentile class interval<br>h is the length of the Quartile/Decile/percentile class interval<br>f is the frequency of the Quartile/Decile/percentile class interval<br>cf is the cumulative frequency of the class interval proceeding the Quartile/Decile/percentile class                                                                                                                                                                                     |                                                   |                                                    |
| <b>Note:</b> In all cases Individual series and discrete series Quartiles, Deciles and percentiles is equal to<br>$Q_i$ = value of $\frac{i(N+1)}{4}$ th term, $D_i$ = value of $\frac{i(N+1)}{10}$ th term, $P_i$ = value of $\frac{i(N+1)}{100}$ th term respectively<br>And in case of continuous series Quartiles, Deciles and percentiles is equal to $Q_i$ = value of $\frac{iN}{4}$ th term,<br>$D_i$ = value of $\frac{iN}{10}$ th term, $P_i$ = value of $\frac{iN}{100}$ th term respectively |                                                   |                                                    |

### 3.1 Example: Individual series

| X                                                                                                                                                                                                            | 5                                                                                                                                                                                     | 15 | 25 | 35 | 45                                                                                                                                                                                                                             | 55 |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|----|----|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| $Q_i$ = value of $\frac{i(n+1)}{4}$ th term where $1 \leq i \leq 3$                                                                                                                                          |                                                                                                                                                                                       |    |    |    |                                                                                                                                                                                                                                |    |
| $D_i$ = value of $\frac{i(n+1)}{10}$ th term where $1 \leq i \leq 10$                                                                                                                                        |                                                                                                                                                                                       |    |    |    |                                                                                                                                                                                                                                |    |
| $P_i$ = value of $\frac{i(n+1)}{100}$ th term where $1 \leq i \leq 100$                                                                                                                                      |                                                                                                                                                                                       |    |    |    |                                                                                                                                                                                                                                |    |
| $Q_1$<br>= value of $\frac{(6+1)}{4}$ th term<br>= value of $\frac{7}{4}$ th term<br>= value of 1.75th term<br><br>$Q_1 = 1st\ term + 0.75(2nd\ term - 1st\ term)$<br>= 5 + 0.75(15 - 5)<br>= 5 + 7.5 = 12.5 | $D_5$ = value of $\frac{5(6+1)}{10}$ th term<br>= value of $\frac{35}{10}$ th term<br>= value of 3.5 th term<br>$D_5 = \frac{3rd\ term + 4th\ term}{2}$<br>= $\frac{25 + 35}{2} = 30$ |    |    |    | $P_{75}$<br>= value of $\frac{75(6+1)}{100}$ th term<br>= value of $\frac{525}{100}$ th term<br>= value of 5.25 th term<br><br>$P_{75} = 5th\ term + 0.25(6th\ term - 5th\ term)$<br>= 45 + 0.25(55 - 45)<br>= 45 + 2.5 = 47.5 |    |

### 3.2 Example: Discrete series

| X                                                                       | 5 | 15 | 25 | 35 | 45 | 55 |               |
|-------------------------------------------------------------------------|---|----|----|----|----|----|---------------|
| Frequency (f)                                                           | 5 | 4  | 3  | 2  | 7  | 9  | $\Sigma f=30$ |
| Cumulative frequency(cf)                                                | 5 | 9  | 12 | 14 | 21 | 30 |               |
| $Q_i$ = value of $\frac{i(N+1)}{4}$ th term where $1 \leq i \leq 3$     |   |    |    |    |    |    |               |
| $D_i$ = value of $\frac{i(N+1)}{10}$ th term where $1 \leq i \leq 10$   |   |    |    |    |    |    |               |
| $P_i$ = value of $\frac{i(N+1)}{100}$ th term where $1 \leq i \leq 100$ |   |    |    |    |    |    |               |

|                                                                                                                                                                                                                                                |                                                                                                                                                                                                                                  |                                                                                                                                                                                                                                               |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $Median = Q_2$<br>$= \text{value of } \frac{2(30+1)}{4} \text{th term}$<br>$= \text{value of } \frac{31}{2} \text{th term}$<br>$= \text{value of } 15.5 \text{th term}$<br>The Cumulative frequency next higher to 15.5 is 21<br>So $Q_2 = 45$ | $D_3 = \text{value of } \frac{3(30+1)}{10} \text{th term}$<br>$= \text{value of } \frac{93}{10} \text{th term}$<br>$= \text{value of } 9.3 \text{th term}$<br>The Cumulative frequency next higher to 9.3 is 12<br>So $D_3 = 25$ | $P_{50} = \text{value of } \frac{50(30+1)}{100} \text{th term}$<br>$= \text{value of } \frac{1550}{100} \text{th term}$<br>$= \text{value of } 15.5 \text{th term}$<br>The Cumulative frequency next higher to 15.5 is 21<br>So $P_{50} = 45$ |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

### 3.3 Example: Continuous series

Same table will be the for Continuous series on replacing X with the class intervals

| Class Intervals          | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 |               |
|--------------------------|------|-------|-------|-------|-------|-------|---------------|
| Frequency (f)            | 5    | 4     | 3     | 2     | 7     | 9     | $\Sigma f=30$ |
| Cumulative frequency(cf) | 5    | 9     | 12    | 14    | 21    | 30    |               |

|                                                                                                                                                                                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                     |                                                                                                                                                                                                                                                                                                                                                                   |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $Q_i = \text{value of } \frac{iN}{4} \text{th term}$<br>$Q_i = L + \frac{\frac{iN}{4} - cf}{f} \times h$<br>where $1 \leq i \leq 3$                                                                                                                                                                                                                   | $D_i = \text{value of } \frac{iN}{10} \text{th term}$<br>$D_i = L + \frac{\frac{iN}{10} - cf}{f} \times h$<br>where $1 \leq i \leq 10$                                                                                                                                                              | $P_i = \text{value of } \frac{iN}{100} \text{th term ,}$<br>$P_i = L + \frac{\frac{iN}{100} - cf}{f} \times h$<br>where $1 \leq i \leq 100$                                                                                                                                                                                                                       |
| $Q_3 =$<br>$= \text{value of } \frac{3N}{4} \text{th term} =$<br>$\text{value of } \frac{90}{4} \text{th term} =$<br>$\text{value of } 22.5 \text{th term}$<br>The Cumulative frequency next higher to 22.5 is 30<br>So 50-60 is $Q_3$ class interval<br>$Q_3 = 50 + \frac{22.5 - 21}{9} \times 10$<br>$= 50 + \frac{15}{9} = 50 + 1.67$<br>$= 51.67$ | $D_7 = \text{value of } \frac{7N}{10} \text{th term}$<br>$= \text{value of } \frac{7 \times 30}{10} \text{th term}$<br>$= \text{value of } 21 \text{st term}$<br>The Cumulative frequency is 21<br>So 40-50 is $D_7$ class interval<br>$D_7 = 40 + \frac{21 - 14}{7} \times 10$<br>$= 40 + 10 = 50$ | $P_{25} = \text{value of } \frac{25N}{100} \text{th term}$<br>$= \text{value of } \frac{25 \times 30}{100} \text{th term}$<br>$= \text{value of } 7.5 \text{th term}$<br>The Cumulative frequency next higher to 7.5 is 9<br>So 10-20 is $P_{25}$ class interval<br>$P_{25} = 10 + \frac{7.5 - 5}{4} \times 10$<br>$= 10 + \frac{25}{4}$<br>$= 10 + 6.25 = 16.25$ |

## IV. MODE

### Notation and terminology used

Mode is generally denoted by symbol 'Z', Rest are same as that of Arithmetic Mean etc.

Mode is that value which occurs most frequently in a statistical distribution.

No mode: if in a distribution each item occurs equal number of times.

Multi-mode: If a few items occur same number of times say twice, thrice called Bi-mode, Tri-mode respectively

#### Individual series

Arrange the items in the ascending or descending order of magnitude. The value with the highest repetition is known as Mode.

#### Discrete series

- a. Inspection Method:** Find the term with highest frequency and the value of the variable corresponding to the term is the mode. The method may not suitable for determination of mode if

the highest frequency is repeated

the gap between the highest frequency and the frequencies proceeding it or succeeding it is very small

the highest frequency occurs in the beginning or at the end of the series

the frequencies of the variable increase or decrease in an erratic or haphazard way

- b. Grouping Method:** is applied when the frequencies are not regular in nature that is there is rise and fall in the values of the frequencies and not possible to locate the value of the mode by inspection properly.

#### Formation of Grouping Table

| X                  | Col I                   | Col II                                                      | Col III                                                                               | Col IV                                                        | Col V                                                                                   | Col VI                                                                                        |  |
|--------------------|-------------------------|-------------------------------------------------------------|---------------------------------------------------------------------------------------|---------------------------------------------------------------|-----------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------|--|
| Write given series | Write given frequencies | Write total of frequencies taking two frequencies at a time | Ignore first frequency and take total of frequencies taking two frequencies at a time | Write total of frequencies taking three frequencies at a time | Ignore first frequency and take total of frequencies taking three frequencies at a time | Ignore first two frequencies and take total of frequencies taking three frequencies at a time |  |

|                                                                                                                                                                                                                                              |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------|--------|---------------------------------------------------------------------------|--------|-------------------------------------------------------------------------------------|--------|------------------------------|
| Mark the maximum values in all the columns                                                                                                                                                                                                   |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| Formation of Analysis Table                                                                                                                                                                                                                  |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| X                                                                                                                                                                                                                                            | Col I                                                                                            | Col II | Col III                                                                   | Col IV | Col V                                                                               | Col VI | Total of tick Marks row wise |
| Tick the rows containing the variable values that produce the highest totals in each column of the grouping table. Afterward, sun the total number of ticks for each row                                                                     |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| The value of the variable which gets the maximum ticks is declared to be the mode of the distribution                                                                                                                                        |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| Continuous Series                                                                                                                                                                                                                            |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| a. Inspection Method: Find the term with highest frequency and the value of the variable corresponding to the term is the mode. The method is not suitable for determination of mode if                                                      |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| the highest frequency is repeated                                                                                                                                                                                                            | the gap between the highest frequency and the frequencies of the adjoining classes is very small |        | the highest frequency occurs in the beginning or at the end of the series |        | the frequencies of the variable increase or decrease in an erratic or haphazard way |        |                              |
| b. Grouping Method: Same as that of in case of discrete series the only difference is that discrete values are replaced by class interval and by this modal class located not the mode , to find mode formula is applied                     |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| First of all locate the modal class by inspection method or Grouping method. Apply the formula                                                                                                                                               |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| $Mode = L + \frac{f - f_0}{2f - f_0 - f_1} \times h$                                                                                                                                                                                         |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| L is the lower limit of the modal class<br>f is the frequency of modal class<br>f <sub>0</sub> is the frequency preceding the modal class<br>f <sub>1</sub> is the frequency following the modal class<br>h is the length of the modal class |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| if above formula gives non valid results or $2f - f_0 - f_1 = 0$<br>then apply                                                                                                                                                               |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| $Mode = L + \frac{\Delta_1}{\Delta_1 + \Delta_2} \times h$                                                                                                                                                                                   |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| Where $\Delta_1 =  f - f_1 $ and $\Delta_2 =  f - f_2 $                                                                                                                                                                                      |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| When upper limit of the modal class is used to find the mode                                                                                                                                                                                 |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| $Mode = U - \frac{f - f_1}{2f - f_0 - f_1} \times h$                                                                                                                                                                                         |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| U is the upper limit of the modal class                                                                                                                                                                                                      |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| if above formula gives non valid results or $2f - f_0 - f_1 = 0$                                                                                                                                                                             |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| $Mode = U - \frac{\Delta_2}{\Delta_1 + \Delta_2} \times h$                                                                                                                                                                                   |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| Where $\Delta_1 =  f - f_1 $ and $\Delta_2 =  f - f_2 $                                                                                                                                                                                      |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| Empirical relation is applicable when mode cannot be calculated in usual way                                                                                                                                                                 |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |
| Mode=3 median -2 mean applicable for Multi Modal series                                                                                                                                                                                      |                                                                                                  |        |                                                                           |        |                                                                                     |        |                              |

#### 4.1 Example: Individual series

|                                                         |                                                |                                             |
|---------------------------------------------------------|------------------------------------------------|---------------------------------------------|
| Four series after arranging the data in ascending order |                                                |                                             |
| <b>X</b>                                                | <b>Arranged data in ascending order</b>        | <b>Mode</b>                                 |
| 1st                                                     | 2, 2, 3, 3, 3, 4, 5, 5, 5, 5, 5, 5, 6, 6, 7    | Uni -Modal series with mode 5               |
| 2nd                                                     | 2, 2, 3, 4, 4, 5, 5, 5, 5, 6, 6, 6, 6, 7, 7    | Bi-Modal series with two modes 5 and 6      |
| 3rd                                                     | 2, 3, 3, 4, 4, 4, 4, 5, 5, 5, 5, 5, 6, 6, 6, 6 | Tri modal series with three modes 4,5 and 6 |
| 4th                                                     | 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13      | Mode is ill defined                         |

#### 4.2 Example: Discrete Series

|                      |   |    |    |    |    |    |
|----------------------|---|----|----|----|----|----|
| <b>X</b>             | 5 | 15 | 25 | 35 | 45 | 55 |
| <b>Frequency (f)</b> | 5 | 4  | 3  | 2  | 7  | 9  |

Max frequency is 9 so mode is 55

#### 4.3 Example: Continuous series

Same table will be the for Continuous series on replacing X with the class intervals

|                 |      |       |       |       |       |       |
|-----------------|------|-------|-------|-------|-------|-------|
| Class Intervals | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 |
| Frequency (f)   | 5    | 4     | 3     | 2     | 7     | 9 max |

Max frequency is 9 so mode class is 50-60

$$Mode = L + \frac{f - f_0}{2f - f_0 - f_1} \times h = 50 + \frac{9 - 7}{2 \times 9 - 7 - 0} \times 10 = 50 + \frac{20}{11} = 50 + 1.82 = 51.82$$

#### 4.4 Example: Discrete series

| X  | Frequency (f) Col I | Col II | Col III | Col IV | Col V  | Col VI | Col I | Col II | Col III | Col IV | Col V | Col VI | Total of ■ |
|----|---------------------|--------|---------|--------|--------|--------|-------|--------|---------|--------|-------|--------|------------|
| 5  | 4                   | 10     |         | 30     |        |        |       |        |         |        |       |        | nil        |
| 15 | 6                   |        | 26      |        | 48 max |        |       |        |         |        | ■     |        | 01         |
| 25 | 20                  | 42     |         |        |        | 65 max |       | ■      |         |        | ■     | ■      | 03         |
| 35 | 22                  | max    | 45      | 62 max |        |        |       | ■      | ■       | ■      | ■     | ■      | 05 max     |
| 45 | 23 max              | 40     | max     |        |        |        | ■     |        | ■       | ■      |       | ■      | 04         |
| 55 | 17                  |        |         |        |        |        |       |        |         | ■      |       |        | 01         |
|    | $N = \sum f = 30$   |        |         |        |        |        |       |        |         |        |       |        |            |
|    |                     |        |         |        |        |        |       |        |         |        |       |        |            |

Maximum number of ■ is 5, so mode is 35

#### 4.5 Example: Continuous series

Same table will be the for Continuous series on replacing X with the class intervals

|                 |      |       |       |       |       |       |
|-----------------|------|-------|-------|-------|-------|-------|
| Class Intervals | 0-10 | 10-20 | 20-30 | 30-40 | 40-50 | 50-60 |
|-----------------|------|-------|-------|-------|-------|-------|

Maximum number of ■ is 5, So Modal class is 30-40

$$Mode = L + \frac{\Delta_1}{\Delta_1 + \Delta_2} \times h \quad \text{Where } \Delta_1 = |f - f_1| \text{ and } \Delta_2 = |f - f_2|$$

Here  $\Delta_1 = |22 - 20| = 2$  and  $\Delta_2 = |23 - 22| = 1$

$$Mode = 30 + \frac{2}{2 + 1} \times 10 = 30 + \frac{20}{3} = 30 + 6.67 = 36.67$$

#### Key note for calculation of Mean, Median/ Other positional Measures and Mode

| Cases/ Type of series/class Interval                                                                | Mean          | Median/ Other positional Measures | Mode      |
|-----------------------------------------------------------------------------------------------------|---------------|-----------------------------------|-----------|
| To arrange data in ascending order or descending order                                              | Not Necessary | Necessary                         | Necessary |
| To convert inclusive series into the exclusive series                                               | Not Necessary | Necessary                         | Necessary |
| To convert unequal class intervals into equal class intervals                                       | Not Necessary | Not Necessary                     | Necessary |
| To convert cumulative frequency distribution 'more than' or 'less than' form, into simple frequency | Necessary     | Necessary                         | Necessary |
| To complete the class intervals in Open end series                                                  | Necessary     | Not Necessary                     | Necessary |
| To construct the class interval in case of mid value series                                         | Not Necessary | Necessary                         | Necessary |

#### 4.6 Example covering Cases/ Type of series/class Interval

| No Example covering cases/ Type of series/class interval |                                    |                 |            |                 |                      |                 |                      |                                           |
|----------------------------------------------------------|------------------------------------|-----------------|------------|-----------------|----------------------|-----------------|----------------------|-------------------------------------------|
| Case I                                                   | Converted Class Interval of Case I | Case II         | Case III   | Case IV         |                      | Case V          |                      | Converted Class Interval For Case II to V |
| Inclusive Class intervals                                | Exclusive Class intervals          | Open end series | Mid values | Class intervals | Cumulative frequency | Class intervals | Cumulative frequency | Class Interval                            |
| 0-9                                                      | 0-9.5                              | Below 10        | 5          | Less than 10    | 5                    | More than 0     | 30                   | 0-10                                      |
| 10-19                                                    | 9.5-19.5                           | 10-20           | 15         | 20              | 9                    | 10              | 25                   | 10-20                                     |
| 20-29                                                    | 19.5-29.5                          | 20-30           | 25         | 30              | 12                   | 20              | 21                   | 20-30                                     |

|       |           |          |    |    |    |    |    |       |
|-------|-----------|----------|----|----|----|----|----|-------|
| 30-39 | 29.5-39.5 | 30-40    | 35 | 40 | 14 | 30 | 18 | 30-40 |
| 40-49 | 39.5-49.5 | 40-50    | 45 | 50 | 21 | 40 | 16 | 40-50 |
| 50-59 | 49.5-59.5 | Above 50 | 55 | 60 | 30 | 50 | 9  | 50-60 |

## V. RANGE, QUARTILE RANGE, DECILE RANGE, PERCENTILE RANGE

### Notation and terminology used

Same as that of used in case of Quartile, Decile and Percentile

|                                                                            |                                                                         |                                                                 |                                                                             |
|----------------------------------------------------------------------------|-------------------------------------------------------------------------|-----------------------------------------------------------------|-----------------------------------------------------------------------------|
| For all the three Individual Series, Discrete Series and Continuous Series |                                                                         |                                                                 |                                                                             |
| Range<br>=largest value-smallest value=<br>$L - S$                         | Quartile Range = $Q_3 - Q_1$                                            | Decile Range<br>= $D_9 - D_1$                                   | Percentile Range<br>= $P_{90} - P_{10}$                                     |
| Coefficient of Range<br>= $\frac{L-S}{L+S}$                                | Coefficient of Quartile<br>Deviation= $\frac{Q_3-Q_1}{Q_3+Q_1}$         | Coefficient of Quartile<br>Deviation= $\frac{D_9-D_1}{D_9+D_1}$ | Coefficient of Quartile<br>Deviation= $\frac{P_{90}-P_{10}}{P_{90}+P_{10}}$ |
|                                                                            | Semi Inter Quartile Range or<br>Quartile Deviation= $\frac{Q_3-Q_1}{2}$ |                                                                 |                                                                             |
| All of these can be easily calculated                                      |                                                                         |                                                                 |                                                                             |

## VI. MEAN DEVIATIONS FROM MEAN, MEDIAN AND MODE

### Notations and Terminology used

Mean Deviations from Mean, Median and Mode are represented by  $MD_{\bar{X}}$ ,  $MD_M$  and  $MD_Z$  respectively,

Rest are the same as used in case of Mean Median and Mode

|                                                                                                                  |                                                                               |                                                                     |                                                                   |
|------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------|---------------------------------------------------------------------|-------------------------------------------------------------------|
| <b>Individual Series</b>                                                                                         | $MD_{\bar{X}} = \sum \frac{ X - \bar{X} }{N}$                                 | $MD_M = \sum \frac{ X - M }{N}$                                     | $MD_Z = \sum \frac{ X - Z }{N}$                                   |
| <b>Discrete Series</b>                                                                                           | $MD_{\bar{X}} = \sum \frac{f X - \bar{X} }{N}$                                | $MD_M = \sum \frac{f X - M }{N}$                                    | $MD_Z = \sum \frac{f X - Z }{N}$                                  |
| <b>Continuous Series</b>                                                                                         | $MD_{\bar{X}} = \sum \frac{f m - \bar{X} }{N}$                                | $MD_M = \sum \frac{f m - M }{N}$                                    | $MD_Z = \sum \frac{f m - Z }{N}$                                  |
| <b>Coefficient of mean deviations For all the three Individual Series, Discrete Series and Continuous Series</b> |                                                                               |                                                                     |                                                                   |
|                                                                                                                  | Coefficient of Mean Deviations<br>from mean, = $\frac{MD_{\bar{X}}}{\bar{X}}$ | Coefficient of Mean Deviations<br>from median<br>= $\frac{MD_M}{M}$ | Coefficient of Mean Deviations<br>from mode<br>= $\frac{MD_Z}{Z}$ |

### 6.1 Example: Individual Series

|                          |                             |    |    |    |    |    |    |        |                                                                   |                                                                                       |
|--------------------------|-----------------------------|----|----|----|----|----|----|--------|-------------------------------------------------------------------|---------------------------------------------------------------------------------------|
|                          | $X \rightarrow$             | 5  | 15 | 25 | 35 | 45 | 55 | Total↓ |                                                                   |                                                                                       |
| $\bar{X}$<br>= 30        | $ X - \bar{X}  \rightarrow$ | 25 | 15 | 5  | 5  | 15 | 25 | 90     | $MD_{\bar{X}} = \sum \frac{ X - \bar{X} }{n} = \frac{90}{6} = 30$ | Coefficient of $MD_{\bar{X}}$<br>= $\frac{MD_{\bar{X}}}{\bar{X}} = \frac{30}{30} = 1$ |
| $M$<br>= 30              | $ X - M  \rightarrow$       | 25 | 15 | 5  | 5  | 15 | 25 | 90     | $MD_M = \sum \frac{ X - M }{n} = \frac{90}{6} = 30$               | Coefficient of $MD_M$<br>= $\frac{MD_M}{M} = \frac{30}{30} = 1$                       |
| Here Mode is not defined |                             |    |    |    |    |    |    |        |                                                                   |                                                                                       |

### 6.2 Example: Discrete series

|     |     |                   |                  |           |            |           |            |
|-----|-----|-------------------|------------------|-----------|------------|-----------|------------|
|     |     | $\bar{X} = 34.67$ |                  | $M = 45$  |            | $Z = 55$  |            |
| $X$ | $f$ | $ X - \bar{X} $   | $f X - \bar{X} $ | $ X - M $ | $f X - M $ | $ X - Z $ | $f X - Z $ |
| 5   | 5   | 29.67             | 148.35           | 40        | 200        | 50        | 250        |
| 15  | 4   | 19.67             | 78.68            | 30        | 120        | 40        | 160        |
| 25  | 3   | 9.67              | 29.01            | 20        | 60         | 30        | 90         |



|    |                   |                                                                                           |                                |                                                                  |                       |                                                                  |                       |
|----|-------------------|-------------------------------------------------------------------------------------------|--------------------------------|------------------------------------------------------------------|-----------------------|------------------------------------------------------------------|-----------------------|
| 35 | 2                 | 0.33                                                                                      | 0.66                           | 10                                                               | 20                    | 20                                                               | 40                    |
| 45 | 7                 | 10.33                                                                                     | 72.31                          | 0                                                                | 0                     | 10                                                               | 70                    |
| 55 | 9                 | 20.33                                                                                     | 182.97                         | 10                                                               | 90                    | 0                                                                | 0                     |
|    | $N = \sum f = 30$ |                                                                                           | $\sum f X - \bar{X}  = 511.98$ |                                                                  | $\sum f X - M  = 490$ |                                                                  | $\sum f X - Z  = 610$ |
|    |                   | $MD_{\bar{X}} = \frac{\sum f X - \bar{X} }{N} = \frac{511.98}{30} = 17.06$                |                                | $MD_M = \frac{\sum f X - M }{N} = \frac{490}{30} = 16.33$        |                       | $MD_Z = \frac{\sum f X - Z }{N} = \frac{610}{30} = 20.33$        |                       |
|    |                   | Coefficient of $MD_{\bar{X}} = \frac{MD_{\bar{X}}}{\bar{X}} = \frac{17.06}{34.67} = 0.49$ |                                | Coefficient of $MD_M = \frac{MD_M}{M} = \frac{16.33}{45} = 0.36$ |                       | Coefficient of $MD_Z = \frac{MD_Z}{Z} = \frac{20.33}{55} = 0.37$ |                       |

### 6.3 Example: Continuous Series

|                 |     |                   |                                                                                           |                         |                                                                     |                          |                                                                     |                          |
|-----------------|-----|-------------------|-------------------------------------------------------------------------------------------|-------------------------|---------------------------------------------------------------------|--------------------------|---------------------------------------------------------------------|--------------------------|
|                 |     |                   | $\bar{X} = 34.67$                                                                         |                         | $M = 41.43$                                                         |                          | $Z = 51.82$                                                         |                          |
| Class Intervals | $m$ | $f$               | $ m - \bar{X} $                                                                           | $f m - \bar{X} $        | $ m - M $                                                           | $f m - M $               | $ m - Z $                                                           | $f m - Z $               |
| 0-10            | 5   | 5                 | 29.67                                                                                     | 148.35                  | 36.43                                                               | 182.15                   | 46.82                                                               | 243.1                    |
| 10-20           | 15  | 4                 | 19.67                                                                                     | 78.68                   | 26.43                                                               | 105.72                   | 36.82                                                               | 147.28                   |
| 20-30           | 25  | 3                 | 9.67                                                                                      | 29.01                   | 16.43                                                               | 49.29                    | 26.82                                                               | 80.46                    |
| 30-40           | 35  | 2                 | 0.33                                                                                      | 0.66                    | 6.43                                                                | 12.86                    | 16.82                                                               | 33.64                    |
| 40-50           | 45  | 7                 | 10.33                                                                                     | 72.31                   | 3.57                                                                | 24.99                    | 6.82                                                                | 47.74                    |
| 50-60           | 55  | 9                 | 20.33                                                                                     | 182.97                  | 13.57                                                               | 122.13                   | 3.18                                                                | 28.62                    |
|                 |     | $N = \sum f = 30$ |                                                                                           | $\sum f m - \bar{X}  =$ |                                                                     | $\sum f m - M  = 497.14$ |                                                                     | $\sum f m - Z  = 571.84$ |
|                 |     |                   | $MD_{\bar{X}} = \frac{\sum f m - \bar{X} }{N} = \frac{511.98}{30} = 17.06$                |                         | $MD_M = \frac{\sum f m - M }{N} = \frac{497.14}{30} = 16.57$        |                          | $MD_Z = \frac{\sum f m - Z }{N} = \frac{571.84}{30} = 19.06$        |                          |
|                 |     |                   | Coefficient of $MD_{\bar{X}} = \frac{MD_{\bar{X}}}{\bar{X}} = \frac{17.06}{34.67} = 0.49$ |                         | Coefficient of $MD_M = \frac{MD_M}{M} = \frac{16.57}{41.43} = 0.40$ |                          | Coefficient of $MD_Z = \frac{MD_Z}{Z} = \frac{19.06}{51.82} = 0.37$ |                          |

## VII. STANDARD DEVIATION

### Notation and terminology used

Standard Deviation is represented by  $\sigma$ . Rest are the same as used in case of Arithmetic Mean

| Standard Deviation in case of Individual series                                           |                                                                                              |                                                                                                              |
|-------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------|
| Direct Method<br>$\sigma = \sqrt{\frac{\sum X^2}{n} - \left(\frac{\sum X}{n}\right)^2}$   | Short-Cut Method<br>$\sigma = \sqrt{\frac{\sum d^2}{n} - \left(\frac{\sum d}{n}\right)^2}$   | Step Deviation Method<br>$\sigma = \sqrt{\frac{\sum d'^2}{n} - \left(\frac{\sum d'}{n}\right)^2} \times c$   |
| Standard Deviation in case of Discrete series                                             |                                                                                              |                                                                                                              |
| Direct Method<br>$\sigma = \sqrt{\frac{\sum fX^2}{N} - \left(\frac{\sum fX}{N}\right)^2}$ | Short-Cut Method<br>$\sigma = \sqrt{\frac{\sum fd^2}{N} - \left(\frac{\sum fd}{N}\right)^2}$ | Step Deviation Method<br>$\sigma = \sqrt{\frac{\sum fd'^2}{N} - \left(\frac{\sum fd'}{N}\right)^2} \times c$ |
| Standard Deviation in case of Continuous series                                           |                                                                                              |                                                                                                              |
| Direct Method<br>$\sigma = \sqrt{\frac{\sum fm^2}{N} - \left(\frac{\sum fm}{N}\right)^2}$ | Short-Cut Method<br>$\sigma = \sqrt{\frac{\sum fd^2}{N} - \left(\frac{\sum fd}{N}\right)^2}$ | Step Deviation Method<br>$\sigma = \sqrt{\frac{\sum fd'^2}{N} - \left(\frac{\sum fd'}{N}\right)^2} \times c$ |
| Coefficient of Standard Deviation and Coefficient of Variation                            |                                                                                              |                                                                                                              |
| Coefficient of Standard Deviation = $\frac{\sigma}{\bar{X}}$                              |                                                                                              | Coefficient of Variation = $\frac{\sigma}{\bar{X}} \times 100$                                               |

Note : 1. Similar to the arithmetic mean , the foundational approach for calculating standard deviation remains same across Individual, Discrete, and Continuous series, the primary distinction lies in computing the  $n, N, d, d'$  for each type of series. Furthermore, because the Individual series contains no frequencies, frequency multiplication is entirely omitted across all three methods. However, multiplying by frequency (f) remains a mandatory step for both Discrete and Continuous series."

2. The Coefficient of Variation is obtained when the Coefficient of Standard Deviation is represented as a percentage.

### 7.1 Example: Discrete Series

| $X$              | $A = 25$<br>$d = m - A$ | $c = 10$<br>$d' = \frac{m - A}{c}$ | $X^2$         | $d^2$         | $d'^2$      |
|------------------|-------------------------|------------------------------------|---------------|---------------|-------------|
| 5                | -20                     | -2                                 | 25            | 400           | 4           |
| 15               | -10                     | -1                                 | 225           | 100           | 1           |
| 25               | 0                       | 0                                  | 625           | 0             | 0           |
| 35               | 10                      | 1                                  | 1225          | 100           | 1           |
| 45               | 20                      | 2                                  | 2025          | 400           | 4           |
| 55               | 30                      | 3                                  | 3025          | 900           | 9           |
| $\Sigma x = 180$ | $\Sigma d = 30$         | $\Sigma d' = 3$                    | $\Sigma 7150$ | $\Sigma 1900$ | $\Sigma 19$ |

  

|                                                                                                                                                                                                                                                                                        |                                                                                                                                                                                                                                                                                                                                                   |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Short-Cut Method</p> $\sigma = \sqrt{\frac{\Sigma d^2}{n} - \left(\frac{\Sigma d}{n}\right)^2}$ $= \sqrt{\frac{1900}{6} - \left(\frac{30}{6}\right)^2} = \sqrt{\frac{1900 \times 6 - 900}{36}} = \sqrt{\frac{11400 - 900}{36}}$ $= \sqrt{\frac{10500}{36}} = \sqrt{291.67} = 17.07$ | <p>Step Deviation Method</p> $\sigma = \sqrt{\frac{\Sigma d'^2}{n} - \left(\frac{\Sigma d'}{n}\right)^2} \times c$ $= \sqrt{\frac{19}{6} - \left(\frac{3}{6}\right)^2} \times 10$ $= \sqrt{\frac{19 \times 6 - 9}{36}} \times 10$ $= \sqrt{\frac{114 - 9}{36}} \times 10$ $= \sqrt{\frac{105}{36}} \times 10 = \sqrt{2.9167} \times 10$ $= 17.07$ |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

### 7.2 Example: Continuous Series

| Class Intervals | Frequency (f)   | (m) | $A = 25$<br>$d = m - A$ | $fd$              | $d^2$ | $fd^2$                | $c = 10'$<br>$d' = \frac{m - A}{c}$ | $fd'$             | $d'^2$ | $fd'^2$              |
|-----------------|-----------------|-----|-------------------------|-------------------|-------|-----------------------|-------------------------------------|-------------------|--------|----------------------|
| 0-10            | 5               | 5   | -20                     | -100              | 400   | 2000                  | -2                                  | -10               | 4      | 20                   |
| 10-20           | 4               | 15  | -10                     | -40               | 100   | 400                   | -1                                  | -4                | 1      | 4                    |
| 20-30           | 3               | 25  | 0                       | 0                 | 0     | 0                     | 0                                   | 0                 | 0      | 0                    |
| 30-40           | 2               | 35  | 10                      | 20                | 100   | 200                   | 1                                   | 2                 | 1      | 2                    |
| 40-50           | 7               | 45  | 20                      | 140               | 400   | 2800                  | 2                                   | 14                | 4      | 28                   |
| 50-60           | 9               | 55  | 30                      | 270               | 900   | 8100                  | 3                                   | 27                | 9      | 81                   |
|                 | $\Sigma f = 30$ |     |                         | $\Sigma fd = 290$ |       | $\Sigma fd^2 = 13500$ |                                     | $\Sigma fd' = 29$ |        | $\Sigma fd'^2 = 135$ |

  

|                                                                                                                                                                                                                                                             |                                                                                                                                                                                                                                                                                                                            |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Short Cut Method</p> $\sigma = \sqrt{\frac{\Sigma fd^2}{N} - \left(\frac{\Sigma fd}{N}\right)^2}$ $= \sqrt{\frac{13500}{30} - \left(\frac{290}{30}\right)^2}$ $= \sqrt{\frac{40500 - 84100}{900}}$ $= \sqrt{\frac{320900}{900}} = \sqrt{356.55} = 18.88$ | <p>Step Deviation method</p> $\sigma = \sqrt{\frac{\Sigma fd'^2}{N} - \left(\frac{\Sigma fd'}{N}\right)^2} \times c$ $= \sqrt{\frac{135}{30} - \left(\frac{29}{30}\right)^2} \times 10 = \sqrt{\frac{405 - 841}{900}} \times 10$ $= \sqrt{\frac{3209}{900}} \times 10 = \sqrt{3.5655} \times 10 = 1.888 \times 10 = 18.88$ |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

|                                                                                                |                                                                                                                                    |
|------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------|
| Coefficient of Standard Deviation = $\frac{\sigma}{\bar{x}} = \frac{18.88}{34.67}$<br>=0.54456 | Coefficient of Variation = $\frac{\sigma}{\bar{x}} \times 100 = \frac{18.88}{34.67} \times 100$<br>= 0.54456 $\times 100 = 54.456$ |
|------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------|

## VII. CONCLUSION

Ultimately, this comparative guide demonstrates that procedural fluency in measures of central tendency and dispersion is best achieved through structured, side-by-side computation. By tracing a single baseline dataset through the Individual, Discrete, and Continuous series frameworks, this paper demystifies the mathematical execution of the mean, median, mode, mean deviation, and standard deviation. This methodological approach directly facilitates the transition from concept to computation. When students observe the logical progression and comparative adaptation of formulas across different data structures, the calculations transition from isolated, intimidating equations into intuitive, step-by-step procedures. By shifting the learner's focus from rote memorization to analytical execution, this guide equips them with the foundational competence and confidence necessary to tackle advanced, real-world data analysis

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