



## Numerical Investigation on the Influence of Turbulence on Limit Cycle Oscillations

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Received 11 July 2015; Accepted 16 July 2015 © The author(s) 2015. Published with open access at [www.questjournals.org](http://www.questjournals.org)

**ABSTRACT:-** This article presents the influence of atmospheric turbulence on the Limit Cycle Oscillations (LCO) that occurs because of a nonlinear coupling between the structural response of an airplane wing and unsteady aerodynamic forces. The presence of nonlinear structural characteristics of modern airplane wing is another crucial reason behind the aero elastic interactions thus resulting self-sustained dynamic vibrations. If an aircraft is flying at an altitude through variable turbulence intensities, then the influence of structural elastic deformations are more important during uncertainty conditions. The response of an airplane against the LCO is not possible to predict through present flow/structural solvers directly. Hence, a novel scheme through loosely coupled approach has been used to predict the aerodynamic load variations in the presence of random turbulence. LCO response of an airfoil made of NACA0012 series is investigated at various Reynolds numbers and different turbulence conditions. The Numerical and computational simulation results are compared to verify the consistency of the proposed approach. The pressure based ideal flow condition is selected for the flow simulation process and the obtained results are significant enough to prove the reliability of the method.

**Keywords:-** Turbulence, Limit Cycle Oscillation, Reynolds number, Aerofoil, CFD.

### I. INTRODUCTION

The airplane wing construction changed from semi-cantilevered configuration to cantilever ones over the past several decades. The benefit of a cantilever wing arrangement is its flexibility to design through cost effective manufacturing techniques. If such a wing configuration is operated at a flight speed above its critical flutter speed then ensuing vibration amplitude is significant<sup>[1]</sup>. Typically, the amplitude of Limit Cycle Oscillations (LCO) is a function of two variables such as the air speed and frequency. The source of the nonlinearity may be fluidic in nature (Eg: shock formation, flow separation, stalling behaviour, etc.) or structural characteristic (buckling, stress-stiffening). These nonlinearities result in a supercritical LCO branch or a subcritical branch<sup>[2]</sup>. Numerical and experimental simulation of LCO's is complicated and intensive process. However, the nonlinearities should be included in the aeroelastic simulation to achieve certain level of modelling fidelity and sophistication<sup>[3]</sup>.

According to the linear theory, a system will continuously go away from the unstable equilibrium point to infinity (or material failure). LCO's are not only necessarily a result of a linear instability but also can be induced by certain disturbances. Basically, if the disturbances are not small, then the response cannot be predicted by theories that are linearized about a nonlinear steady state. Depending on the vibration amplitude of the LCO, the structure may or may not experience immediate failure yet, for an airplane LCO's pose substantial problems in their own right. This vibration also causes fatigue problems and reducing the useful life of the wing structure. Consequently, efficient prediction of LCO is vital during design phase, especially for airplanes flying near the limits of the linear assumptions. Texas A&M University developed the Nonlinear Aeroelastic Test Apparatus (NATA) consists of NACA 64A010 and supercritical NLR 7301 airfoils to investigate the linear and nonlinear aeroelastic behavior experimentally<sup>[3]</sup>. NATA provides a wing mount (made of rigid NACA 0015 wing section) that offers for 2 Degrees of Freedom (DoF) movement in pitch and plunge motions<sup>[4]</sup>.

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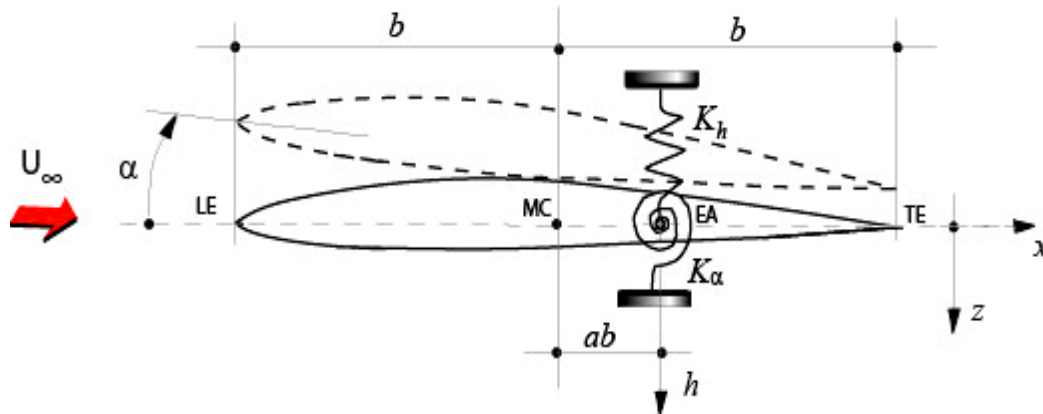
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The limit cycle amplitudes are very sensitive to variations in angles of attack<sup>[5]</sup>. The 'buzz' responses are observed in a number of practical situations and implications for airplane safety purposes. Sedaghatet al (2000) provides the experimental and theoretical characteristics of LCOs for a three DoF airfoil system with a freeplay in the flap<sup>[6]</sup>. It was the first successful initiative to quantify the LCO behavior in the bending-torsion coupling modes. Later, various theoretical, computational, and experimental capabilities to analyze the LCO are exposed. In particular, aerodynamic flows with large shock motions and flow separation are discussed through Volterra series Reduced Order Modeling (ROM) approach for the purpose of flutter prediction, aeroelastic control design, and aeroelastic design optimization<sup>[7]</sup>. However, this approach is unsuccessful while applied to other aeroelastic phenomena, such as aerodynamically induced LCO's<sup>[8]</sup>. Especially with certain high-performance airplane configurations, nonlinearities in the aeroelastic system induce abnormal structural behavior such as the observed store-induced LCO's<sup>[9]</sup>.

Watkins et al (2010) tested the flat airfoils at a Reynolds Number (RN) of  $7.5 \times 10^4$  in the presence of different percentage turbulence conditions. When the length scale of turbulent region was increased with the constant intensity, the slope of lift curve was increased significantly and it reduces maximum lift coefficient ( $C_{L,max}$ )<sup>[10]</sup>. If an airplane is cruising continuously in low turbulence, then the prevailing response would be LCO and it cannot be classified as gust response. Nevertheless, if the airplane were flying in severe turbulence, then the gust response would be primarily that due to turbulence with bursts of LCO. The flow separation is also severe and the wing has high-frequency panel-type modes of vibrations<sup>[11]</sup>. In this article, a simplified analysis procedure is developed to quantify the influence of turbulence on the basic aerodynamic coefficients by CFD. For low and severe turbulence conditions, the initiation of LCO boundary can be well established through the proposed aeroelastic analysis by the means of computational flow simulations. The presence of LCO would probably have little or no effect on wing loads that could result in structural damage<sup>[12]</sup>. However, in the secondary structure, it is very sensitive to fatigue damage caused by LCO loadings.

## II. MATHEMATICAL MODELLING

A two DoF aeroelastic system modeled as an airfoil section that allows pitching and plunging motion is illustrated in Figure 1. In the proposed methodology, the pitch and plunge frequencies alone considered for simplifying the frequency response analysis. For this model, the governing equations for the 2-DoF aeroelastic system can be written as follows,



**Figure 1. Representation of 2-DoF pitching and plunging wing section**

$$m\ddot{h} + m x_\alpha b \ddot{\alpha} + c\dot{h} + k_h h = L(t) + L_d(t) + L_c(t) \quad (1)$$

$$I_\alpha \ddot{\alpha} + m x_\alpha b \ddot{h} + c_\alpha \dot{\alpha} + k_\alpha (\alpha) \alpha = M(t) + M_d(t) + M_c(t) \quad (2)$$

Where,  $\alpha$  = Angle of attack

$K_h$  = Bending Stiffness

$K_\alpha$  = Torsional Stiffness

Most of the research works reported in the past decade have been utilized the flat plates and symmetrical airfoils for analyzing the LCO properties computationally. Since, the influence of change in RN on the dynamic pressure is a required quantity, the present analysis also done using the symmetrical airfoil (NACA 0012) configuration. The basic airfoil selection procedure is followed based on the thickness,  $C_L$ , drag coefficient ( $C_D$ ), camber and chord length<sup>[13]</sup>. Airplane performance mainly depends on  $C_L$  and  $C_D$  magnitudes that are influenced in proportion with the change in RN. The bending and torsional stiffness magnitudes of Aluminum alloy 6061-T6 material (ISTM Standard) is assumed for the purpose Finite Element Analysis. Once

the fundamental frequencies for the selected mode shapes are computed then the pressure fluctuations are related with the appropriate twisting/bending modes. In the case of experimental validation, the analysis will be carried out by establishing the similar boundary condition inside the wind tunnel through the same airfoil fabricated with suitable material and dimensional similarity.

### III. COMPUTATIONAL MODELING

A 3D model of commercial transport airplane wing using NACA 0012 airfoil is prepared by CATIA modeling tool. Numerical investigation of flow and structural properties of this model is prepared by ANSYS workbench. It offers a comprehensive range of engineering simulation solution sets providing access to virtually any field of engineering simulation that a design process requires. The complete design specifications of CATIA model are listed in Table 1. The 2D and 3D views of the wing configuration are presented in Figure 2. Structural properties of the model such as stiffness, empty weight, Young's Modulus and Poisson's ratio are computed separately by the Mechanics of materials approach.

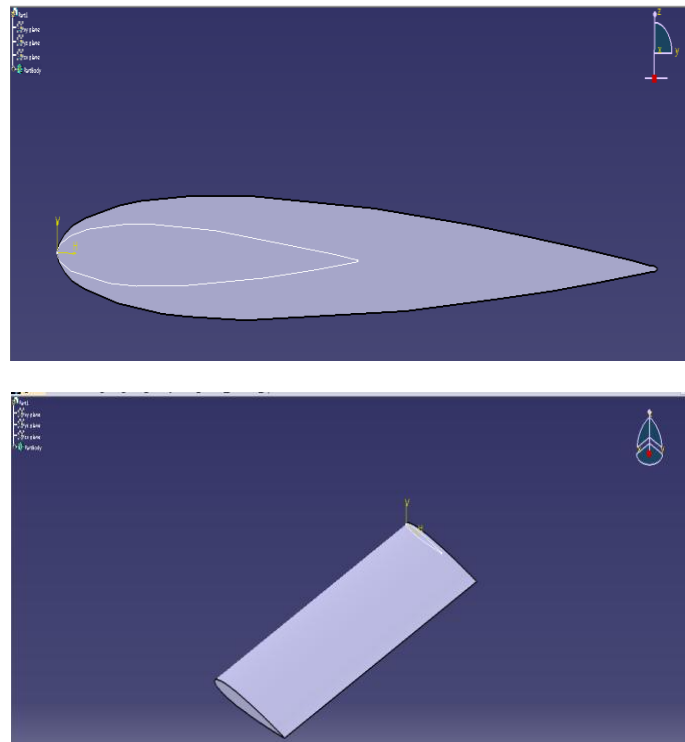


Figure 2. 2D and 3D wing model made of NACA 0012 airfoil

#### 3.1 BOUNDARY CONDITION

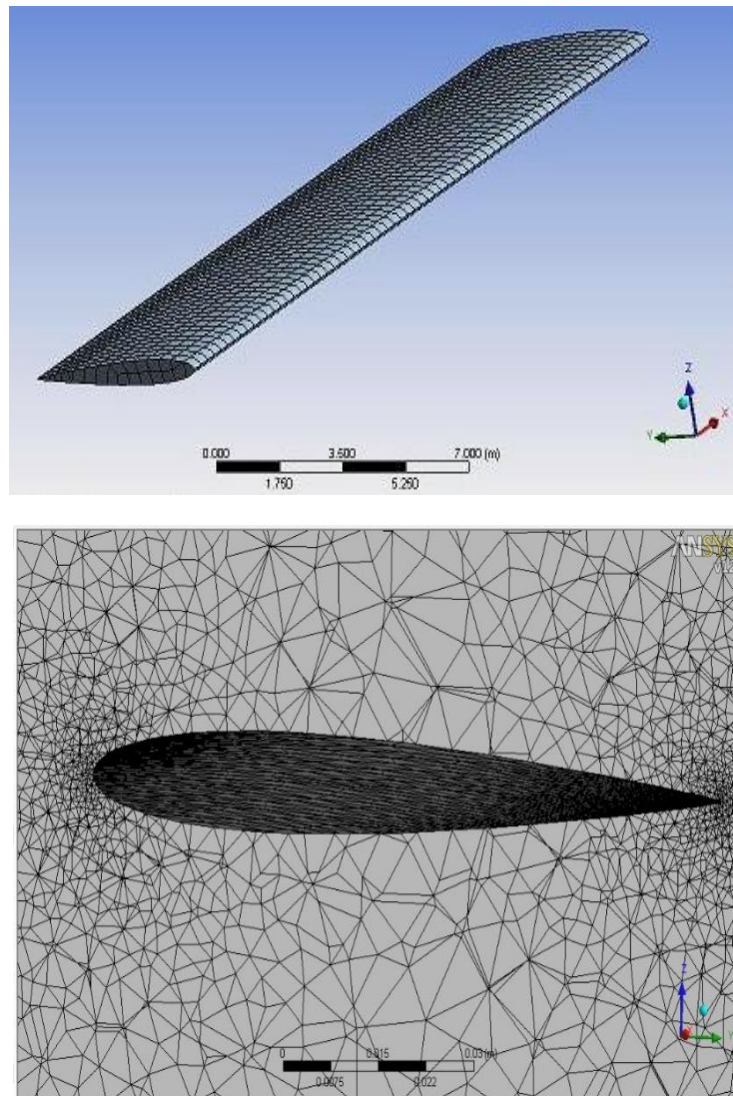
The boundary condition assumed for the prediction of fundamental frequencies using Finite Element Analysis tool (FEA) is given in Table 1. In the input boundary condition, pressure based ideal flow cases are considered without any friction. Turbulence Intensity (TI) is calculated at different Re and at various altitudes.

Sl.NO	Specifications	Values	Assumptions	Values
1.	Chord	10.2 cm	Speed of Sound, $a$	328 m/s
2.	Span	27.33 cm	Velocity, $v$	238.3 m/s
3.	Area	0.057 m <sup>2</sup>	Mach number $M$	0.7
4.	Mass	0.609 kg	Dynamic viscosity, $\mu$	17.93 x 10 <sup>-6</sup> Ns/m <sup>2</sup>
5.	Material	Al 6061-T6	Density, $\rho$	2710 kg/m <sup>3</sup>

Table 1. Specifications for CATIA modeling and assumptions for flow simulations

#### 3.2 ANSYS MODELING

The wing model is exported to FEA tool for the meshing and simulation process. The solutions are obtained for the given boundary condition at various Re with an operating Mach number about 0.7. Fine meshing is prepared for the FEA of wing model with an element sizing of 1.5 mm as highlighted in Figure 3. The unstructured tetrahedral cells<sup>[14]</sup> of fine elements formed in the meshing pattern with slightly coarse mesh near the maximum thickness location for fluid domain meshing.



**Figure3. Structural and Fluid domain Meshes for the wing model**

Figure 3 shows the full scale drawing of the cross section of NACA 0012 airfoil and the conditions surrounding the airfoil (upper and lower surface = wall). Based on the flow analysis domain, the mesh pattern consists of 3,14,289 nodes and for FEA 34,300 nodes are prepared with SOLID 185 element. For most aeroelastic applications, where the magnitudes of viscous and turbulent effects are similar, it is preferable to keep the range of  $y^+$ , smallest as possible between 5 and 30. This is to ensure that the simulation runs as close as possible to the airfoil. For this simulation, the  $y^+$  value denoted by the flow solver is about 12.

## IV. RESULTS AND DISCUSSION

### 4.1 FREQUENCY RESULTS

Pre-stressed wing model is used to determine the frequency of vibrating body when it has the aerodynamic loading conditions. It clearly depicts that the static air loads imposed on the wing is the key motivation for getting high frequency forced vibrations. Hence, the pre-stressed modal analysis is used for the selected wing configuration to ensure the usable range of dynamic vibration frequencies. The result of modal analysis is displayed in Figure 5.

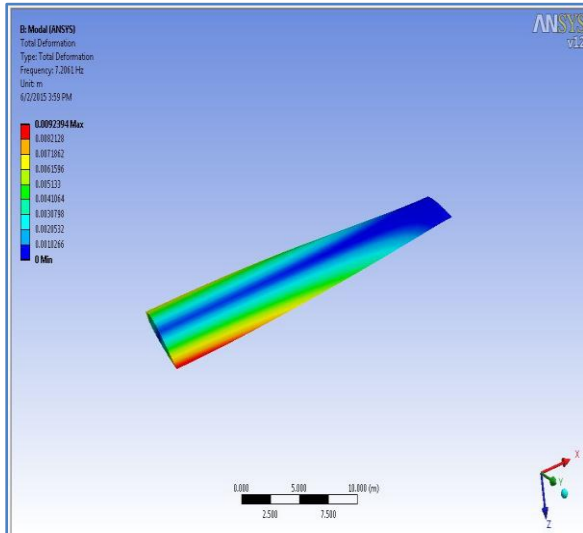


Figure 4. Angle of attack Vs Frequency

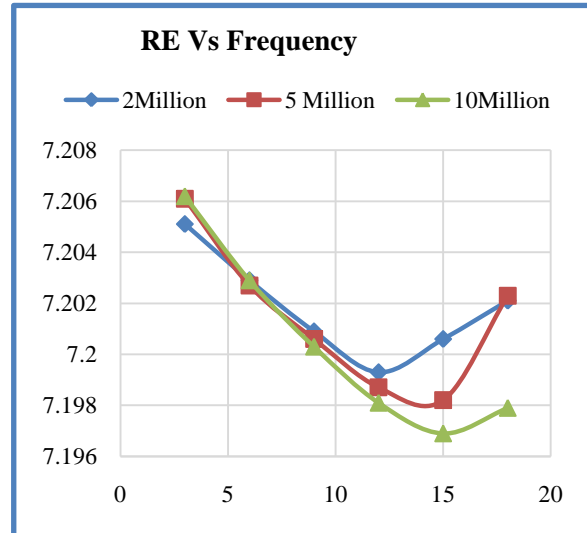


Figure 5. Frequency at bending mode of wing

Frequency is the number of occurrences of a repeating event per unit time. It is also referred to as temporal frequency, which emphasizes the contrast to spatial frequency and angular frequency. The period is the duration of one cycle in a repeating event, so the period is the reciprocal of the frequency. Frequencies of different mode shapes are plotted in Figure 4. When coming into the bending mode shapes wings are getting high deflection due to the forced vibration at their tip chords.

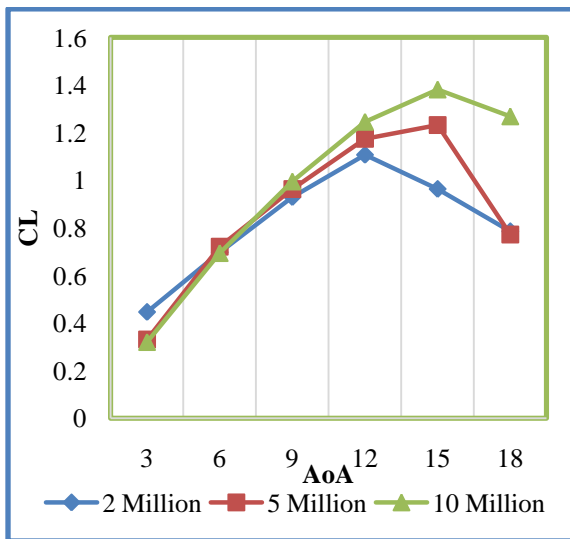


Figure 6. Reynolds Number Vs  $C_L$

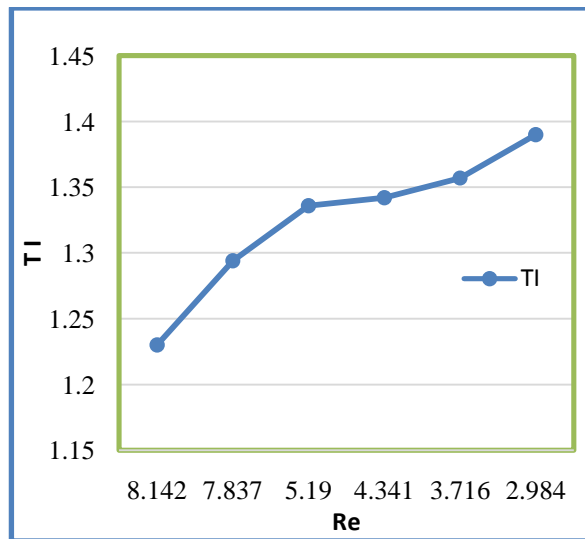


Figure 7. Turbulence Intensity Vs Re

Figure 6 shows the lift coefficient computed for the model kept at various angles of attack and RN. At various RN, the coefficient of lift changes considerably and when RN is about 10 million it reaches the maximum. It is well known that the incremental RN could also influence the  $C_D$  magnitude that tends the airplane to damp out the LCO<sup>[16]</sup>. Similarly, Figure 7 represents the TI at various Reynolds numbers over the symmetric airfoil. It shows a striking result that increment in RN decreases the Turbulence intensity approximately in a linear manner. Further, the pitch and plunge oscillations prevail according to the local stiffness of the wing section as described in the mathematical model.

#### 4.2 VELOCITY AND PRESSURE CONTOURS

At 0° Angle of attack, the wind elements collide with the airfoil stagnation points as shown in Figure 8. Since it is symmetric in nature, velocity distribution of the wind is approximately same on both upper and lower surface of the airfoil. Therefore, the equal pressure distributions on the upper and lower layer represent zero resultant aerodynamic force that can be negligible. However, at various RN this pressure

distribution possess high TI that creates a shift in location along the chord line for peaks and valleys of velocities over the airfoil.

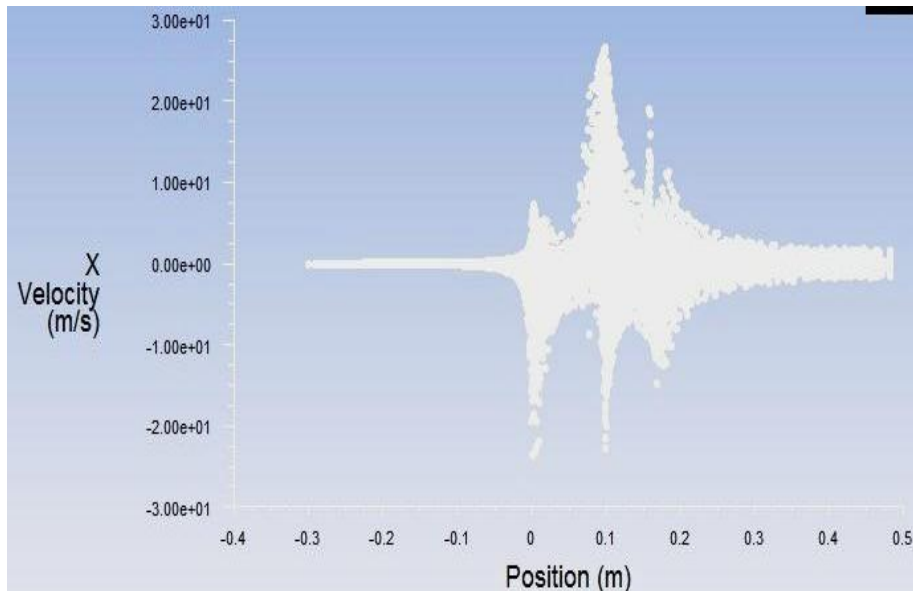


Figure 8. Velocity distribution at Reynolds number = 2 million

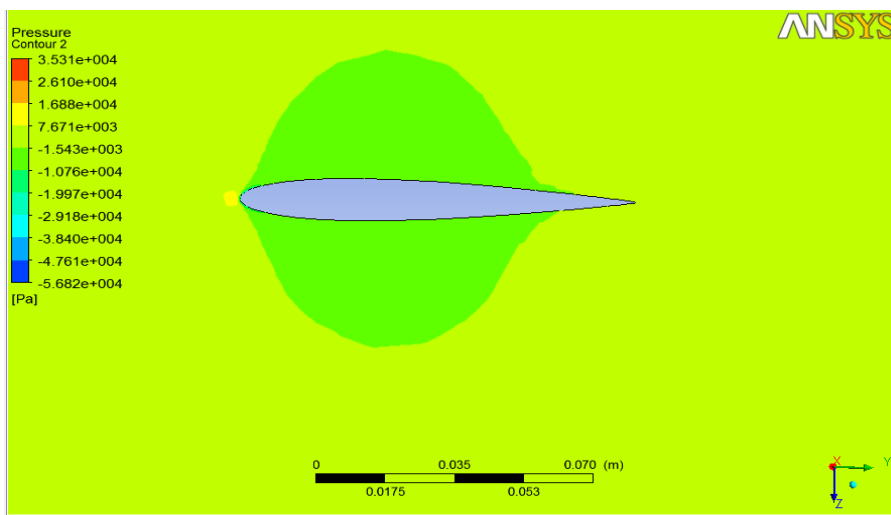
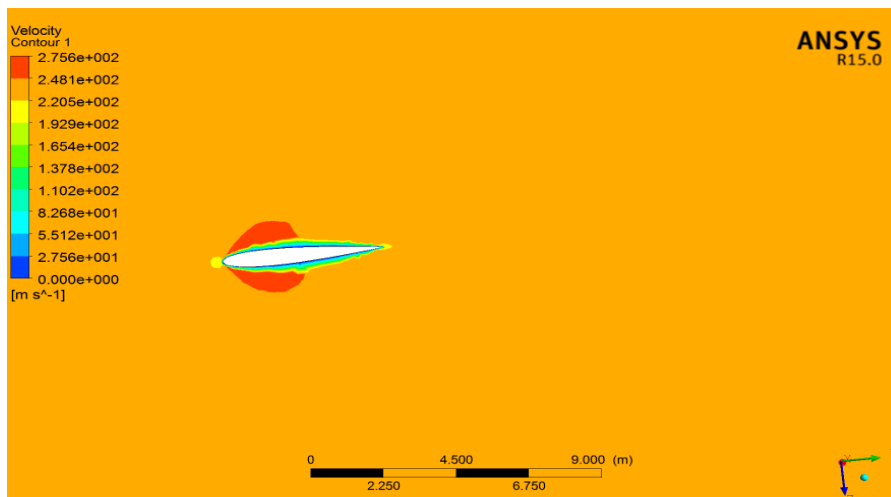


Figure 9. Velocity and pressure distribution contours

Figure 9 shows the flow of velocity and pressure distribution contour over the wing model at sea level conditions. The maximum velocity is reached at the maximum thickness location of the airfoil as expected about 275.4 m/s. At different high RN input conditions, the velocity distribution is modified even at zero angle of attack as stated above. This differential aerodynamic forces tend to initiate low amplitude oscillations based on the free stream Mach number. At high AoA, this similar velocity/pressure distribution on both upper and lower layer of airfoils is broken and amplitude of LCO begins to increase. Hence, the present investigation provides striking information that for the same pressure on both the surface of airfoil with different RN flow induced oscillations begin to occur.

## V. CONCLUSIONS

The present article is intended to compute the influence of structural excitation modes on the LCO's. Through modal analysis, the fundamental frequencies are observed for the assumed wing model at sea level conditions. Through the baseline studies, aerodynamically induced LCO and its boundaries of the prototypical wing model can be evaluated by a transonic wind tunnel testing. The coefficient of lift and drag at various altitudes are calculated from the CFD simulations to quantify the influence of RN on the aerodynamic quantities. The frequency response at various RN conditions is plotted along with the response of TI for different AoA. The pressure, velocity, and turbulent kinetic energy are evaluated from FLUENT flow solver for various degrees of turbulence. In future, the Wind Tunnel experiments can be conducted using the same wing model to calculate the LCO response.

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